

# BÀI TẬP GIÁO KHOA

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# Toán 11

Bài 32

CÁC QUY TẮC TÍNH ĐẠO HÀM

**Câu 1**

$$y' = \left(\frac{1}{4}x^4\right)' - \left(\frac{2}{3}x^3\right)' + (5x)' - (\sqrt{2})'$$

$$y' = x^3 - 2x^2 + 5$$

**Câu 2**

$$y' = \cos x + \sin x$$

$$y^2 + (y')^2 = (\sin x - \cos x)^2 + (\cos x + \sin x)^2$$

$$y^2 + (y')^2 = (\sin^2 x - 2\sin x \cos x + \cos^2 x) + (\cos^2 x + 2\sin x \cos x + \sin^2 x)$$

$$y^2 + (y')^2 = 2(\sin^2 x + \cos^2 x) = 2 \text{ (đpcm)}$$

**Câu 3**

$$y' = 4(2x^2 - 3x + 1)^3 \cdot (2x^2 - 3x + 1)'$$

$$y' = 4(2x^2 - 3x + 1)^3 \cdot (4x - 3)$$

$$y' = (16x - 12)(2x^2 - 3x + 1)^3$$

**Câu 4**

$$y' = -(\sqrt{x^2 + 1})' \cdot \sin(\sqrt{x^2 + 1})$$

$$y' = -\frac{x}{\sqrt{x^2 + 1}} \cdot \sin(\sqrt{x^2 + 1})$$

**Câu 5**

$$f'(x) = \frac{1}{\cos^2 x} - \frac{1}{\sin^2 x}$$

$$f'\left(\frac{\pi}{4}\right) = \frac{1}{\cos^2\left(\frac{\pi}{4}\right)} - \frac{1}{\sin^2\left(\frac{\pi}{4}\right)}$$

$$f'\left(\frac{\pi}{4}\right) = \frac{1}{1/2} - \frac{1}{1/2} = 2 - 2 = 0$$

**Câu 6**

$$y' = \frac{2(x+4) - 1(2x-3)}{(x+4)^2}$$

$$y' = \frac{2x+8-2x+3}{(x+4)^2} = \frac{11}{(x+4)^2}$$

**Câu 7**

$$y' = 3x^2 - 6x$$

$$y' = 0 \Leftrightarrow 3x(x-2) = 0$$

$$x = 0 \text{ hoặc } x = 2$$

**Câu 8**

$$y_0 = y(2) = \frac{2+2}{2-1} = 4$$

$$y' = \frac{-3}{(x-1)^2} \Rightarrow k = y'(2) = \frac{-3}{(2-1)^2} = -3$$

$$\text{PTTT: } y - 4 = -3(x - 2) \Leftrightarrow y = -3x + 10$$

**Câu 9**

$$y' = 3x^2 - 2$$

$$k = y'(1) = 3(1)^2 - 2 = 1$$

$$\text{PTTT: } y - (-1) = 1(x - 1) \Leftrightarrow y = x - 2$$

**Câu 10**

$$y_0 = \sin(\pi) + 1 = 1$$

$$y' = 2 \cos(2x)$$

$$k = y'\left(\frac{\pi}{2}\right) = 2 \cos(\pi) = -2$$

$$\text{PTTT: } y - 1 = -2\left(x - \frac{\pi}{2}\right) \Leftrightarrow y = -2x + \pi + 1$$

